

# Descriptive Statistics: What Data Can & Can Not Tell You

## Class Syllabus

### What Is Statistics

What it is, Why it Matters, and How this Course is Different



Read: **FREE PREVIEW: Your Authors**

Optional



Watch: **FREE PREVIEW: Getting Started**

Optional



Read: **FREE PREVIEW: Randomness & Probability**

Optional



Read: **FREE PREVIEW: Populations and Samples**

Optional



Read: **Parameters & Statistics**

Optional



Listen: **Representative Samples**

Optional

### How Do Any of Us Know Anything?

Theoretical vs. Empirical Frameworks for Knowledge



Read: **Organizing Observations**

Optional



Take: **Confirmation Bias**

Optional



Read: **Was Julius Ceasar a Real Person?**

Optional

# Kinds of Data

Data Type and Measurement Level



Read: **Quantitative vs. Qualitative Data**

Optional



Watch: **Levels of Data**

Optional

# Absolute and Relative Comparisons

Thinking carefully about subtraction and division



Read: **Absolute Change**

Optional



Read: **Relative Change**

Optional



Read: **What You Now Know**

Optional



Submit: **Your Turn: Your First Big Bad Assignment**

30 Points

# A Very Quick Hop Through Classical Probability

Only What We Absolutely Need



Read: **What is Probability?**

Optional



Read: **Experiments, Trials, Outcomes, and Sample Spaces**

Optional



Watch: **Events, Singular Events, and the Empty Set**

Optional



Watch: **Classical Probability**

Optional



Watch: **When You Change the Rules a Little...**

Optional



Watch: **The Ultra-Useful Complement Rule**

Optional

## Intuition Builder: You Lost Your Wallet. How Do You Find It (Before Someone Else Does)?



Read: **Set Up**

Optional



Watch: **"Where Do I Remember Last Having It?"**

Optional



Read: **Pragmatism: Don't Build A Complicated Model**

Optional

# Free Tools That We'll Need For Our Journey

Desmos, Google Sheets, R



Submit: **Your Turn: Check Out Desmos!**

30 Points



Watch: **Why Not Excel for Spreadsheets?**

Optional



Submit: **Your Turn: Spreadsheet Basics in Google Sheets**

30 Points



Watch: **Downloading R and R Studio for Free**

Optional



Read: **Why Use the R Programming Language?**

Optional

## Data: Making it Up, Finding it, Modifying it

We're going to do a lot of cool things with data. Let's have some fun with making some of it up ourselves, and also a couple places where we can find real data.



Submit: **Your Turn: Making Up a Scenario and Its Data**

Optional



Submit: **Your Turn: Watch Me Download Free Data**

100 Points



Read: **Accessing Data from FRED on Unemployment**

Optional



Submit: **Your Turn: Collect Data on the "Misery Index"**

30 Points



Read: **Quick Warning: Getting Data from Different Sources**

Optional

## Intuition Builder: Bring Out the Scales



Read: **Which Has More Mass?**

Optional



Watch: **Which Has More Mass - Take Two!**

Optional

## Empirical Probability

Likelihood Derived Through Careful, Independent Observation



Watch: **Empirical Probability**

Optional



Read: **Empirical Probability v. Classical Probability**

Optional



Watch: **The Law of Large Numbers and the Law of Small Numbers**

Optional

## Intuition Builder: How Long Will You Have to Wait?

C'mon, Greg!



Read: **Taking Reciprocals**

Optional



Read: **Just a Long-Run Average Frequency**

Optional

# Building Frequency Tables With Qualitative Data

Frequency, Relative Frequency, Cumulative Relative Frequency

 Watch: **Scenario: How Do Employees Commute?**  
Optional

 Watch: **Building a Frequency Table in Google Sheets**  
Optional

 Read: **Relative Frequency**  
Optional

 Watch: **Cumulative Relative Frequency**  
Optional

 Watch: **What YOU Just Learned is Huge**  
Optional

 Submit: **Your Turn: Build Your Own Frequency Table**  
30 Points

## Visualizing Qualitative Data

 Watch: **Venn Diagrams**  
Optional

 Watch: **Bar Charts in All Their Glory**  
Optional

 Submit: **Your Turn: Pie Charts (Should We Use Them?)**  
30 Points

 Read: **Pictographs...Tread Carefully (But Don't Knock 'em)**  
Optional

## Intuition Builder: Which is More Likely?

 Read: **Heads 5 Times in a Row v. Snake Eyes**  
Optional

 Watch: **{Heads, Tails, Heads} or {Tails, Tails, Tails}?**  
Optional

 Read: **Unlikely Does Not Mean Impossible!**  
Optional

# Random Variables

Turning Events Into Numbers

 Watch: **Defining a Random Variable**  
Optional

 Read: **Turning Categorical Outcomes into Random Variables**  
Optional

 Watch: **Turning Quantitative Events into Random Variables**  
Optional

 Submit: **Your Turn: Construct Your Own Random Variables!**  
40 Points

 Watch: **Really Quick! Why the Hype?**  
Optional

## Discrete and Continuous Random Variables

 Watch: **What are Discrete Data?**  
Optional

 Watch: **What are Continuous Data?**  
Optional

 Read: **Discrete v. Continuous Data**  
Optional

 Read: **Discrete and Continuous Random Variables**  
Optional

 Submit: **Your Turn: Model Your Own Discrete Random Variable**

 Submit: **Your Turn: Model a Continuous Random Variable**

# Extending Frequency Tables to Quantitative Data

How the processes are similar, and likely more useful to us



Watch: **Discrete Frequency Tables**

Optional



Submit: **Your Turn: Building and Interpreting the Frequency Table**

30 Points



Read: **Using Ranges to Construct a Frequency Table for a Continuous Random...**

Optional



Watch: **Building Ranges Appropriately (Spoiler Alert!)**

Optional

# Intuition Builder: How Will That Stock You Like Do Over the Next Week?



Submit: **Your Turn: Download the Data Together, and Plot out Returns**

30 Points



Read: **Lots of Data V. Recent Data**

Optional

# Visualizing Quantitative Data

Segway into Descriptive Statistics



Submit: **The Line Graph**

Optional



Submit: **The Area Chart**

Optional



Submit: **The Scatterplot**

100 Points



Read: **When It's Best to Use a Line Graph, Area Chart, or Scatterplot**

Optional



Watch: **The Histogram - How It's Different Than a Bar Chart**

Optional



Submit: **Your Turn: Make a Histogram in Desmos**

30 Points



Submit: **Your Turn: Make a Histogram in Google Sheets**

30 Points

## Exam 1



Take: **Exam**

## Collective Exhaustion and Mutual Exclusivity

Exactly One Event is Going to Win Out



Read: **Grouping Events**

Optional



Watch: **Collective Exhaustion**

Optional



Watch: **Mutual Exclusivity**

Optional



Watch: **Putting Together What We Know**

Optional

# Intuition Builder: How Many Swallows Does a Spring Make?



Read: **What is Inference?**

Optional



Watch: **Flirtatious Banter as Inference**

Optional

## Probability Distributions



Watch: **Review of Discrete v. Continuous Data & Random Variables**

Optional



Read: **Seeing Old Ideas in a New Way**

Optional



Read: **At Last - Probability Distributions Defined**

Optional



Read: **What Does a Discrete Probability Distribution Look Like?**

Optional



Read: **What Does a Continuous Probability Distribution Look Like?**

Optional



Read: **Which One is Not a Probability Distribution?**

Optional

## Probability Mass Functions



Read: **Review: Relative Frequency**

Optional



Read: **Probability Mass Function**

Optional



Read: **How are Relative Frequency and Probability Mass Different Ideas?**

Optional

# Important Notation Part I

Summation Notation



Read: **Do You Know These Symbols?**

Optional



Watch: **Adding a Bunch of Things Together: Discrete Case**

Optional



Read: **Adding a Bunch of Numbers Together: Continuous Case**

Optional

# Cumulative Mass Functions



Read: **Review: Cumulative Relative Frequency**

Optional



Read: **Cumulative Mass Functions**

Optional



Read: **Grouping Probabilities**

Optional



Read: **That Mighty Useful Complement Rule**

Optional



Read: **Important Skill: Slicing and Dicing**

Optional

# Hall of Fame Distributions

Meet and Greet - Nothing too Serious



Read: **Hall of Fame Discrete Distributions**

Optional



Read: **Hall of Fame Continuous Distributions**

Optional



Watch: **What About The Gnarly Distributions?**

Optional

# Intuition Builder: Is It Random?



Watch: **Determinism v. Random Walk**

Optional



Read: **Randomness is Not an All-or-Nothing Proposition**

Optional

## Probability Density Functions (PDFs)

What they Look Like Mathematically, and Computing them with Free Technology



Read: **Frequency Tables with Continuous Data**

Optional



Read: **Quick Review: Probability Mass Functions**

Optional



Watch: **The Paradox of Continuity**

Optional



Read: **The Intuition Behind Probability Density**

Optional



Read: **Defining the PDF**

Optional



Watch: **The Leap from PDF to Probability**

Optional



Watch: **Examples of PDFs**

Optional



Watch: **Two Rules for PDFs**

Optional



Read: **PDF or PMF?**

Optional

# Cumulative Density Functions (CDFs)

The continuous path from 0% to 100%. Don't worry - most of these paths are quite short!

 Watch: **CDFs: What Do They Look Like, and Why Do We Need Them?**  
Optional

 Take: **Very Quick Review: CRF and CMF**  
Optional

 Read: **Quick Review: Probability Density Functions**  
Optional

 Read: **Very Quick Review: CMF as Very Helpful Analogue to CDF**  
Optional

 Read: **What the CDF Tells Us**  
Optional

 Watch: **Calculating a CDF On Computers**  
Optional

 Read: **Two Rules for CDFs**  
Optional

 Watch: **Where Do We Get the Formulas for CDFs?**  
Optional

## Two Important Uses of CDFs

Complement Rule and area between two cdf values

 Read: **That Mighty Useful Complement Rule (CDF Edition)**  
Optional

 Watch: **Slicing and Dicing: Calculating the Probability  $X$  Falls on Interval  $[a,b]$**   
Optional

 Watch: **Watching  $\Pr[a < X < b]$  in Google Sheets**  
Optional

 Watch: **The Complement Rule in Google Sheets**

# Features of Distributions

Thinking About the Shape of Our Data



Read: **Very Brief Comparison Between Discrete & Continuous Distributions**

Optional



Read: **Shaping Up Our Data: Shape & Outliers**

Optional



Read: **Shaping Up Our Data: Center & Spread**

Optional



Watch: **Treat it Like an Etch-a-Sketch**

Optional

## Intuition Builder: Which Would You Rather Own?



Read: **Two Investments - You Decide**

Optional



Read: **Experiencing V. Remembering Self**

Optional

## Important Notation Part II

Population v. Sample



Read: **Review Population V. Sample**

Optional



Watch: **Notation that We Use for the Population Parameters**

Optional



Read: **Notation that We use for our Sample**

Optional



Watch: **Recognize the Importance of What You Just Learned**

Optional

# Exam #2

Take: **Exam #2**

## Measures of Central Tendency

Crystalizing How Our Data Cluster, Center, and Balance

 Watch: **Introducing the Concept**  
Optional

 Watch: **The Mode**  
Optional

 Watch: **The Median**  
Optional

 Watch: **Benefits of the Mode(s) V. the Median**  
Optional

 Watch: **Outliers - What Do We Do with Them?**  
Optional

 Watch: **The Mean**  
Optional

 Read: **Why We Care About the Mean So Much**  
Optional

 Watch: **Three Ways to Take an Arithmetic Mean**  
Optional

 Read: **Want to Try? Compute an Arithmetic Mean**  
Optional

 Read: **Computing the Mean for Grouped Data**  
Optional

# Expected Value

In One or More Variables



Watch: **Review: Random Variables Copy**

Optional



Watch: **What's an Expected Value?**

Optional



Read: **Review: Three Ways to Take an Arithmetic Mean**

Optional



Watch: **Calculating an Expected Value: The Categorical Case**

Optional



Read: **Calculating Discrete Random Variables**

Optional



Read: **Calculating an Expected Value: The Continuous Case**

Optional



Read: **Example of an Expected Value of Continuous Random Variable**

Optional



Read: **Expected Value as the Balance Point of Our Random Variable**

Optional

## Intuition Builder: Would You Rather Divide a Fixed Pot of Money Between Two, Ten, or One Hundred People?



Read: **When the Numerator Stays the Same, but the Denominator Changes**

# Degrees of Freedom

What they are, When and Why they Matter



Read: **The Simple Version**

Optional



Read: **Population and Degrees of Freedom**

Optional



Watch: **A Sample and Degrees of Freedom**

Optional

# Intuition Builder: Which Sleep Schedule Would You Rather Have?



Read: **Get Your Rest!**

Optional

## Measures of Dispersion

Min, Max, Range, Variance, and Standard Deviation



Watch: **Introducing the Concept**

Optional



Read: **Min, Max, & Range: Advantages and Limitations**

Optional



Read: **Measures of Dispersion: Take Two**

Optional



Read: **Setting Up Population Variance**

Optional



Watch: **Population Variance**

Optional



Watch: **A Hop, Skip and Jump to the Population Standard Deviation**

Optional



Read: **When to Use the Variance, and When to Use Standard Deviation**

Optional



Watch: **Population Dispersion Measures to Sample Dispersion Measures**

Optional



Read: **What Have You Learned?**

Optional

# Intuition Builder: As Long As A Few Of 'Em Love You

Making Dispersion Your Friend

▶ Watch: **You Don't Have to Get Everyone on Your Side**

▶ Watch: **You Don't Have to Get Everyone on Your Side Copy**

## Combining What We Know

Coefficient of Variation measures consistency within our data. Z-scores measure exceptionalism within or between data sets (they're a really big deal).

▶ Watch: **Coefficient of Variation - Demonstrating Consistency of the Data as a ...**

▶ Watch: **Z-scores: Measuring Exceptionalism Within and Between Data Sets**

☑ To-Do: **Ready to Go On?**

☰ Take: **Can you Find the COV?**

☰ Take: **Calculating the Mean and the Standard Deviation**

# Correlation is not Causation (Except for When It is)

How we calculate it, and what it tells us

 Watch: **Moving From Variation to Association**

 Watch: **Introduction to Covariance**

 Read: **Turning Covariance into Something We Can (Mis)use**

 Take: **Covariance and Correlation Recap**

 Watch: **Visualizing Correlation**

 Watch: **Correlation Abuse: Most Wanted**

 Read: **Correlation is Not Causation, Except a Lot of the Time it Is**

# Fleshing Out Our Probability Skills

Independence and Intersections

 Read: **Dependence and Independence Defined**

 Watch: **Intersections and Independent Random Variables**

 Take: **Probability Review**

 Read: **Putting it Together (Mutually Exclusive and Independent Events)**

 Take: **Independence Tests**

 Listen: **Correlation = 0 Does Not Mean Independent**

# The Simplest Distributions to Understand

Geometric Distribution, Uniform Distribution(s)

 Read: **The Most Intuitive: The Discrete Uniform Distribution**

 Read: **Expected Value of a Discrete Uniform Random Variable**

 Take: **Calculating the Intersection of Independent Random Variables**

 Watch: **The Logic Behind the Geometric Distribution**

 Read: **Interpreting the EV and the SD for the Geometric Distribution**

 Watch: **The logic behind the uniform distribution**

 Read: **Behind the Scenes - EV and the SD for the Uniform Distribution**

## When Distributions Pair

Working with the Poisson and Exponential Distributions. We find a cool relationship between the exponential and the geometric distributions.

 Watch: **That Special Number "e"**

 Read: **The Poisson Distribution**

 Take: **Geometric Distributions**

 Watch: **The Poisson Distribution in Action**

 Watch: **Pairing Distributions**

 Read: **Comparing the Geometric and Exponential Distributions**

 Read: **Mean and Variance - Exponential Probability Distribution**

## Career Moves: Subjective Probability

 Watch: **What is Subjective Probability?**

# The Big, Bad, Beautiful Bell Curve.

Why is it such a big deal?

☰ Take: **Optional General Review**

☰ Read: **Core Properties of a Perfect Normal Distribution**

▶ Watch: **The PDF Explained**

▶ Watch: **Build a Bell Curve in Desmos!**

☰ Read: **The CDF explained**

☰ Read: **Warning: Huge Misconceptions About the Bell Curve**

☰ Take: **Putting It All Together**

☰ Take: **Just to Make Sure You are Up to Speed.**

# Does the Famous Empirical Rule Always Apply?

And Why It Matters

📄 Take: **What Does the Empirical Rule State?**

📄 Read: **Testing the Empirical Rule - Small Sample or Population**

📺 Watch: **Testing the Empirical Rule**

📄 Read: **Chebychev's Rule**

📄 Take: **Wrap Up**

📺 Watch: **A Big Deal!**

📄 Take: **Just Making Sure You're Hanging in There!**

## Just One Moment?

Actually, we should understand four.

📺 Watch: **"Moments" Give Us a Language About the Shape of Our Distribution**

📄 Read: **Mean and Variance**

📺 Watch: **Skew Explained**

📺 Watch: **What is Kurtosis?**

📺 Watch: **"Moments" Give Us a Language About the Shape of Our Distribution C...**

# Important Extensions (Teaser)

We don't want to overload you. We owe you at least a quick introduction.

☰ Read: **Extending the Exponential Distribution to Accommodate Multiple Obser...**

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☰ Read: **Extending the Geometric Distribution to Accommodate Combinations o...**

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☰ Read: **Poisson and its Connections to the Binomial Distribution**

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▶ Watch: **The Normal Distribution ---> T-Distribution Family**

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▶ Watch: **What Gives? Why Not Include More?**

## Warnings As We Conclude

Pitfalls to Avoid

☰ Read: **Lying with Statistics (Split into Error in Collecting / Presenting / Interpre...**

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☰ Read: **Errors in Decision Making**

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☰ Read: **Indispensable Takeaways (and Why We Maybe Like to Go With Our Gut)**

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☰ Read: **Error in Collecting Data**

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☰ Read: **Error in Presenting Data**

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☰ Read: **Error in Interpreting Data**

# You Did It!

The Most Important Things That You Have Learned

 Read: **The Most Important Ideas from this Class**

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 Take: **Scary Final Exam...**

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 Watch: **Video Congratulations and Wrap Up**

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 Read: **The Most Important Ideas from this Class Copy**